

PHYS 350 E&M

Exam 5

March 29, 2017

Name J. CDALY

1. The rectangular loop carrying a current, I_1 , is close to a long straight wire carrying a current I_2 as shown in Figure 1. Find the force on the loop.

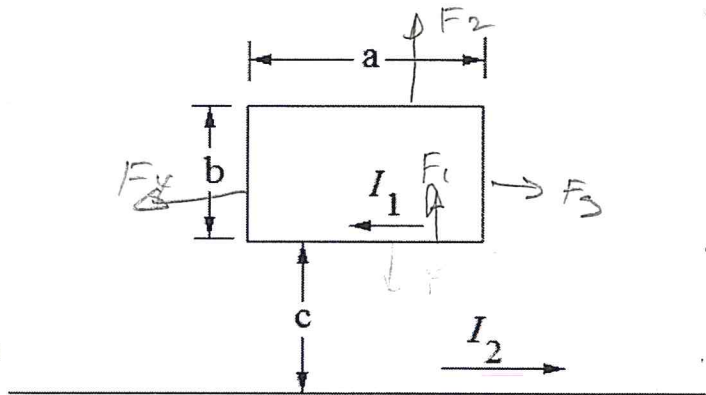


Figure 1

$$\vec{B} = \frac{\mu_0 I_2}{2\pi r} \hat{\phi} \quad \text{out of page}$$

$$\vec{F} = \vec{F}_1 + \vec{F}_2$$

$F_3 + F_4$ on the sides cancel

$$F = ILB$$

$$\vec{F}_1 = \frac{\mu_0 I_1 I_2 a}{2\pi c} \hat{r}$$

$$\vec{F}_2 = -\frac{\mu_0 I_1 I_2 a}{2\pi (c+b)} \hat{r}$$

$$\vec{F} = \frac{\mu_0 I_1 I_2 a}{2\pi} \left[\frac{1}{c} - \frac{1}{(c+b)} \right] \hat{r}$$

up
away from
 I_2

GRADES

100, 100

92

84
82

55

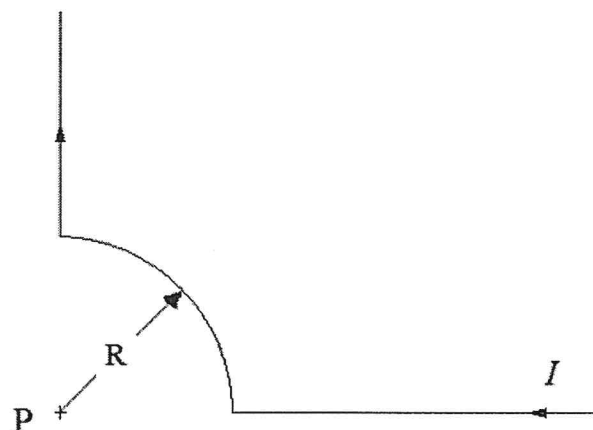
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2. A current, I , flows along a long straight horizontal wire, then around a circular arc, and then up a long straight wire. Find the magnetic field at center of curvature of the circular arc, point P, in Figure 2.

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{\ell} \times \hat{r}}{r^2}$$



The B field produced by the straight section is zero at P. Since $I d\vec{\ell} \times \hat{r} = 0$

The circular arc produces a magnetic field at P.

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\ell}{R^2}$$

$$d\ell = R d\theta$$

$$B = \int d\vec{B} = \frac{\mu_0 I}{4\pi R} \int_0^{\pi/2} d\theta$$

$$\vec{B} = \frac{\mu_0 I}{8R} \hat{n} \quad \text{out of page} \\ \text{By RHR}$$

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3. A current, I , flows in the inner conductor and out the outer conductor of the coaxial cable shown in Figure 3. Find the magnetic field in the region between the conductors ($a < r < b$).

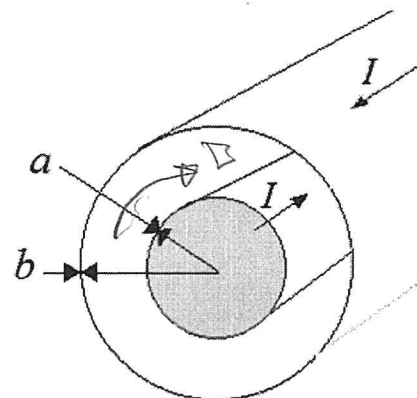


Figure 3

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I_{enc}$$

$$\oint \vec{B} \cdot d\vec{\ell} = 2\pi r B_\theta$$

$$\text{For } a < r < b$$

$$I_{enc} = I$$

$$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{\theta}$$

